

DELFT UNIVERSITY OF TECHNOLOGY
Faculty of Civil Engineering and Geosciences

Soil Mechanics I – MOCK EXAM I

CT1091

BSc EXAMINATION 2012

ANSWER BOOK

FOURTH PERIOD

Answer ALL Questions
(Note that the questions carry unequal marks)

Other instructions

Write your name on each sheet

Clearly identify the answer in the answer box

Question No.	Workings	Answer
1a	From inspection, assuming that river is connected to permeable sand and sand is significantly more permeable than the clay, i.e. an upward flow problem:	1.5 m excavation
1b	Specific discharge, q (m/s), is $q = -k \frac{dh}{dL} = -3.6 \times 10^{-8} \frac{(1.5 - 2.5)}{1.5} = 2.4 \times 10^{-8} \text{m/s}$ Discharge (m ³ /s) = $qA = 2.4 \times 10^{-8} \times 6 \times 150 = 0.0000216$ 0.0000216 x 3600 = 0.078 m ³ /hour	0.078 m ³
1c	Liquefaction can occur when effective stress equals zero. Total stresses at the base of the excavation = $(4 - d) \times 19$ Where d is the depth of excavation. Pore water pressure in the excavation = $(4 - 1.5) \times 10 = 25 \text{ kN/m}^2$ Therefore: $d = 4 - (25/19) = 2.7\text{m}$	2.7m
1d	Again, liquefaction can occur when effective stress equals zero. Total stresses at the base of the excavation = $(4 - 2.5) \times 19 = 28.5 \text{ kN/m}^2$ Where d is the depth of excavation. Critical pore water pressure in the excavation = $(4 - d_w) \times 10$ Therefore: $d_w = 4 - (28.5/10) = 1.15\text{m}$	1.15m

Question No.	Workings	Answer
2a	$\gamma = W/V$ $W = W(\text{kg}) * 10 = 557 / 1000 * 10 = 5.57\text{N}$ $V = 300 \times \pi \times 40^2 / 4 = 376\,990 \text{ mm}^3 = 0.000377 \text{ m}^3$ $\gamma = 5.57 / 0.000377 = 14775 \text{ N/m}^3 = 14.8 \text{ kN/m}^3$	14.8 kN/m ³
2b	<p>Clay on sieve size 1 μm, Silt on sieve size 2 μm, Sand above Therefore $V_{\text{clay}} = 17 \text{ ml}$, $W_{\text{clay}} = 32 / 1000 * 10 = 0.32 \text{ N}$</p> <p>$V_{\text{silt}} = 35 \text{ ml}$, $W_{\text{silt}} = 78 / 1000 * 10 = 0.78 \text{ N}$</p> <p>$V_{\text{sand}} = (61+63+12+5) = 141 \text{ ml}$, $W_{\text{sand}} = (117+133+28+9) / 1000 * 10 = 2.87 \text{ N}$</p>	$V_{\text{clay}} = 17 \text{ ml}$ $W_{\text{clay}} = 0.32 \text{ N}$ $V_{\text{silt}} = 35 \text{ ml}$, $W_{\text{silt}} = 0.78 \text{ N}$ $V_{\text{sand}} = 141 \text{ ml}$ $W_{\text{sand}} = 2.87 \text{ N}$
2c	<p>Mass of Peat = 502 – 397 = 105g $V = 105 / 1000 / 1100 \times 100^3 = 95.5 \text{ ml}$ $\%_{\text{peat}} = 95.5 / 377 \times 100 = 25.3\%$ $\%_{\text{sand}} = 141 / 377 \times 100 = 37.4\%$</p> <p>Mass of water = 557 – 502 = 55g $V = 55 \times 1 = 55 \text{ ml}$ $\%_{\text{water}} = 55 / 377 \times 100 = 14.6\%$ $V = 377 - (17+35+141+95.5+55) = 33.5 \text{ ml}$ $\%_{\text{air}} = 33.5 / 377 \times 100 = 8.9\%$</p>	$\%_{\text{peat}} = 25.3\%$ $\%_{\text{sand}} = 37.4\%$ $\%_{\text{water}} = 14.6\%$ $\%_{\text{air}} = 8.9\%$
2d	$n = V_p / V_t$ $= (55+33.5) / 377 = 0.235 * 100 = 23.5\%$	23.5%
2e		
2f	<p>From figure: $D_{10} = 2.5$, $D_{60} = 102$ $C_u = 102 / 2.5 = 41$, Well graded</p> <p>S – sand (or accept Pt – peat) W – well graded</p>	$C_u = 41$ S W

Question No.	Workings	Answer
3a		
3b	<p>Mid height of the clay:</p> $\sigma = (225+129)/2 = 177 \text{ kPa}$ $\sigma' = (100+86.5)/2 = 93.25 \text{ kPa}$ <p>After embankment, pwp can dissipate therefore stresses are increase by $3.5 \times 18 = 63 \text{ kPa}$ at all locations. Assumption is 'wide' embankment.</p> $\sigma = 177+63 = 240 \text{ kPa}$ $\sigma' = 93.25 + 63 = 156.25 \text{ kPa}$	$\sigma = 177 \text{ kPa}$ $\sigma' = 93.25 \text{ kPa}$ <p>After</p> $\sigma = 240 \text{ kPa}$ $\sigma' = 156.25 \text{ kPa}$
3c	<p>3 layers of 2 m each. Final settlement so no increased pwp or consolidation.</p> <p>Centres of layers (NAP, m): -9.5, -11.5, -13.5</p> $\text{Initial } \sigma' = \sigma'_{-8.5} + (d) \frac{\sigma'_{-14.5} - \sigma'_{-8.5}}{6}$ $\sigma'_{-9.5} = 88.75 \text{ kPa}, \sigma'_{-11.5} = 93.25 \text{ kPa}, \sigma'_{-13.5} = 97.75 \text{ kPa}$ <p>Strain: $\epsilon = \frac{1}{c_p} \ln\left(\frac{\sigma'}{\sigma'_1}\right)$</p> $\epsilon_{-9.5} = \frac{1}{15} \ln\left(\frac{88.75+63}{88.75}\right) = 0.036, \epsilon_{-11.5} = 0.034, \epsilon_{-13.5} = 0.033$ <p>Deformation, $u = 2x\epsilon$</p> $\text{Total deformation} = 2 \times (\epsilon_{-13.5} + \epsilon_{-11.5} + \epsilon_{-9.5}) = 0.21 \text{ m}$	0.21m

Question No.	Workings	Answer																														
4a	Use the flexible plate formulation, $r=0$: $\sigma_{zz} = p \left[1 - \frac{z^3}{(\sqrt{z^2+a^2})^3} \right] = 150 \left[1 - \frac{z^3}{(\sqrt{z^2+7.5^2})^3} \right] =$ $\sigma_{zz2} = 147 \text{ kPa}, \sigma_{zz7} = 102 \text{ kPa}, \sigma_{zz15} = 42.7 \text{ kPa}$	$\sigma_{zz2} = 147$ kPa, $\sigma_{zz7} = 102$ kPa, $\sigma_{zz15} = 42.7$ kPa																														
4b	Use the strip foundation equation, $x=0$: $p=150 \times w / (2 \times \text{StripWidth}) = 150 \times 15 / (2 \times 0.5) = 2250 \text{ kN/m}^2$ $\sigma_{zz} = \frac{2p}{\pi} \left\{ \tan^{-1} \left(\frac{a}{z} \right) + \frac{az}{a^2 + z^2} \right\} = \frac{2 \times 2250}{\pi} \left\{ \tan^{-1} \left(\frac{0.25}{z} \right) + \frac{0.25z}{0.25^2 + z^2} \right\}$ $\sigma_{zz2} = 354 \text{ kPa}, \sigma_{zz7} = 102 \text{ kPa}, \sigma_{zz15} = 47.7 \text{ kPa}$	$\sigma_{zz2} = 354$ kPa, $\sigma_{zz7} = 102$ kPa, $\sigma_{zz15} = 47.7$ kPa																														
4c	Pad foundation. Use point load as no dimensions are given, also will be similar. Would accept if reasonable dimensions were used e.g. 2m diameter. $P = 150 \times (w/2) \times \text{spacing} = 150 \times 7.5 \times 12 = 13500 \text{ kPa}$ $\sigma_{zz} = \frac{3P}{2\pi z^2}$ $\sigma_{zz2} = 1611 \text{ kPa}, \sigma_{zz7} = 131 \text{ kPa}, \sigma_{zz15} = 28.6 \text{ kPa}$	$\sigma_{zz2} = 1611$ kPa, $\sigma_{zz7} = 131$ kPa, $\sigma_{zz15} = 28.6$ kPa																														
4d	Recognise that the stresses calculated in 4b are in the centres of the prescribed layers. Therefore: <table border="1" data-bbox="331 1263 1177 1541"> <thead> <tr> <th>Layer centre</th> <th>σ_1</th> <th>σ_{zz}</th> <th>Strain</th> <th>thickness</th> <th>disp</th> </tr> </thead> <tbody> <tr> <td>2</td> <td>32</td> <td>354</td> <td>0.0094</td> <td>4</td> <td>0.037</td> </tr> <tr> <td>7</td> <td>112</td> <td>102</td> <td>0.0024</td> <td>6</td> <td>0.015</td> </tr> <tr> <td>15</td> <td>240</td> <td>47.7</td> <td>0.0007</td> <td>10</td> <td>0.007</td> </tr> <tr> <td colspan="5" style="text-align: right;">total=</td> <td>0.059m</td> </tr> </tbody> </table> Therefore 6 cm so acceptable.	Layer centre	σ_1	σ_{zz}	Strain	thickness	disp	2	32	354	0.0094	4	0.037	7	112	102	0.0024	6	0.015	15	240	47.7	0.0007	10	0.007	total=					0.059m	6 cm Acceptable
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