

**DELFT UNIVERSITY OF TECHNOLOGY**  
**Faculty of Civil Engineering and Geosciences**

**Soil Mechanics I – MOCK EXAM I**

**CT1091**

**BSc EXAMINATION 2012**

ANSWER BOOK

FOURTH PERIOD

Answer ALL Questions  
(Note that the questions carry unequal marks)

Other instructions  
**Write your name on each sheet**

**Clearly identify the answer in the answer box**

Question No.	Workings	Answer
1a	From inspection, assuming that river is connected to permeable sand and sand is significantly more permeable than the clay, i.e. an upward flow problem:	1.5 m excavation
1b	<p>Specific discharge, <math>q</math> (m/s), is</p> $q = -k \frac{dh}{dL} = -3.6 \times 10^{-8} \frac{(1.5 - 2.5)}{1.5} = 2.4 \times 10^{-8} \text{m/s}$ <p>Discharge (m<sup>3</sup>/s) = <math>qA = 2.4 \times 10^{-8} \times 6 \times 150 = 0.0000216</math>  <math>0.0000216 \times 3600 = 0.078 \text{ m}^3/\text{hour}</math></p>	0.078 m <sup>3</sup>
1c	<p>Liquefaction can occur when effective stress equals zero.</p> <p>Total stresses at the base of the excavation = <math>(4 - d) \times 19</math>  Where <math>d</math> is the depth of excavation.</p> <p>Pore water pressure in the excavation = <math>(4 - 1.5) \times 10 = 25 \text{ kN/m}^2</math></p> <p>Therefore:</p> $d = 4 - (25/19) = 2.7\text{m}$	2.7m
1d	<p>Again, liquefaction can occur when effective stress equals zero.</p> <p>Total stresses at the base of the excavation = <math>(4 - 2.5) \times 19 = 28.5 \text{ kN/m}^2</math> Where <math>d</math> is the depth of excavation.</p> <p>Critical pore water pressure in the excavation = <math>(4 - d_w) \times 10</math></p> <p>Therefore:</p> $d_w = 4 - (28.5/10) = 1.15\text{m}$	1.15m

Question No.	Workings	Answer
2a	$\gamma = W/V$ $W = W(\text{kg}) * 10 = 557 / 1000 * 10 = 5.57\text{N}$ $V = 300 \times \pi \times 40^2 / 4 = 376\,990 \text{ mm}^3 = 0.000377 \text{ m}^3$ $\gamma = 5.57 / 0.000377 = 14775 \text{ N/m}^3 = 14.8 \text{ kN/m}^3$	14.8 kN/m <sup>3</sup>
2b	<p>Clay on sieve size 1 <math>\mu\text{m}</math>, Silt on sieve size 2 <math>\mu\text{m}</math>, Sand above</p> <p>Therefore <math>V_{\text{clay}} = 17 \text{ ml}</math>, <math>W_{\text{clay}} = 32 / 1000 * 10 = 0.32 \text{ N}</math></p> <p><math>V_{\text{silt}} = 35 \text{ ml}</math>, <math>W_{\text{silt}} = 78 / 1000 * 10 = 0.78 \text{ N}</math></p> <p><math>V_{\text{sand}} = (61+63+12+5) = 141 \text{ ml}</math>, <math>W_{\text{sand}} = (117+133+28+9) / 1000 * 10 = 2.87 \text{ N}</math></p>	$V_{\text{clay}} = 17 \text{ ml}$ $W_{\text{clay}} = 0.32 \text{ N}$  $V_{\text{silt}} = 35 \text{ ml}$ , $W_{\text{silt}} = 0.78 \text{ N}$  $V_{\text{sand}} = 141 \text{ ml}$ $W_{\text{sand}} = 2.87 \text{ N}$
2c	<p>Mass of Peat = 502 – 397 = 105g  <math>V = 105 / 1000 / 1100 \times 100^3 = 95.5 \text{ ml}</math>  <math>\%_{\text{peat}} = 95.5 / 377 \times 100 = 25.3\%</math>  <math>\%_{\text{sand}} = 141 / 377 \times 100 = 37.4\%</math></p> <p>Mass of water = 557 – 502 = 55g  <math>V = 55 \times 1 = 55 \text{ ml}</math>  <math>\%_{\text{water}} = 55 / 377 \times 100 = 14.6\%</math>  <math>V = 377 - (17+35+141+95.5+55) = 33.5 \text{ ml}</math>  <math>\%_{\text{air}} = 33.5 / 377 \times 100 = 8.9\%</math></p>	$\%_{\text{peat}} = 25.3\%$ $\%_{\text{sand}} = 37.4\%$ $\%_{\text{water}} = 14.6\%$ $\%_{\text{air}} = 8.9\%$
2d	$n = V_p / V_t$ $= (55+33.5) / 377 = 0.235 * 100 = 23.5\%$	23.5%
2e		
2f	<p>From figure: <math>D_{10} = 2.5</math>, <math>D_{60} = 102</math>  <math>C_u = 102 / 2.5 = 41</math>, Well graded</p> <p>S – sand (or accept Pt – peat) W – well graded</p>	$C_u = 41$  S W

Question No.	Workings	Answer
3a		
3b	<p>Mid height of the clay:</p> $\sigma = (225+129)/2 = 177 \text{ kPa}$ $\sigma' = (100+86.5)/2 = 93.25 \text{ kPa}$ <p>After embankment, pwp can dissipate therefore stresses are increase by <math>3.5 \times 18 = 63 \text{ kPa}</math> at all locations. Assumption is 'wide' embankment.</p> $\sigma = 177+63 = 240 \text{ kPa}$ $\sigma' = 93.25 + 63 = 156.25 \text{ kPa}$	$\sigma = 177 \text{ kPa}$ $\sigma' = 93.25 \text{ kPa}$ <p>After</p> $\sigma = 240 \text{ kPa}$ $\sigma' = 156.25 \text{ kPa}$
3c	<p>3 layers of 2 m each. Final settlement so no increased pwp or consolidation.</p> <p>Centres of layers (NAP, m): -9.5, -11.5, -13.5</p> $\text{Initial } \sigma' = \sigma'_{-8.5} + (d) \frac{\sigma'_{-14.5} - \sigma'_{-8.5}}{6}$ $\sigma'_{-9.5} = 88.75 \text{ kPa}, \sigma'_{-11.5} = 93.25 \text{ kPa}, \sigma'_{-13.5} = 97.75 \text{ kPa}$ <p>Strain: <math>\epsilon = \frac{1}{c_p} \ln\left(\frac{\sigma'}{\sigma'_1}\right)</math></p> $\epsilon_{-9.5} = \frac{1}{15} \ln\left(\frac{88.75+63}{88.75}\right) = 0.036, \epsilon_{-11.5} = 0.034, \epsilon_{-13.5} = 0.033$ <p>Deformation, <math>u = 2x\epsilon</math></p> $\text{Total deformation} = 2 \times (\epsilon_{-13.5} + \epsilon_{-11.5} + \epsilon_{-9.5}) = 0.21 \text{ m}$	0.21m

Question No.	Workings	Answer																														
4a	Use the flexible plate formulation, $r=0$ : $\sigma_{zz} = p \left[ 1 - \frac{z^3}{(\sqrt{z^2+a^2})^3} \right] = 150 \left[ 1 - \frac{z^3}{(\sqrt{z^2+7.5^2})^3} \right] =$ $\sigma_{zz2} = 147 \text{ kPa}, \sigma_{zz7} = 102 \text{ kPa}, \sigma_{zz15} = 42.7 \text{ kPa}$	$\sigma_{zz2} = 147$ kPa, $\sigma_{zz7} = 102$ kPa, $\sigma_{zz15} = 42.7$ kPa																														
4b	Use the strip foundation equation, $x=0$ : $p=150 \times w / (2 \times \text{StripWidth}) = 150 \times 15 / (2 \times 0.5) = 2250 \text{ kN/m}^2$ $\sigma_{zz} = \frac{2p}{\pi} \left\{ \tan^{-1} \left( \frac{a}{z} \right) + \frac{az}{a^2 + z^2} \right\} = \frac{2 \times 2250}{\pi} \left\{ \tan^{-1} \left( \frac{0.25}{z} \right) + \frac{0.25z}{0.25^2 + z^2} \right\}$ $\sigma_{zz2} = 354 \text{ kPa}, \sigma_{zz7} = 102 \text{ kPa}, \sigma_{zz15} = 47.7 \text{ kPa}$	$\sigma_{zz2} = 354$ kPa, $\sigma_{zz7} = 102$ kPa, $\sigma_{zz15} = 47.7$ kPa																														
4c	Pad foundation. Use point load as no dimensions are given, also will be similar. Would accept if reasonable dimensions were used e.g. 2m diameter. $P = 150 \times (w/2) \times \text{spacing} = 150 \times 7.5 \times 12 = 13500 \text{ kPa}$ $\sigma_{zz} = \frac{3P}{2\pi z^2}$ $\sigma_{zz2} = 1611 \text{ kPa}, \sigma_{zz7} = 131 \text{ kPa}, \sigma_{zz15} = 28.6 \text{ kPa}$	$\sigma_{zz2} = 1611$ kPa, $\sigma_{zz7} = 131$ kPa, $\sigma_{zz15} = 28.6$ kPa																														
4d	Recognise that the stresses calculated in 4b are in the centres of the prescribed layers. Therefore: <table border="1" data-bbox="331 1263 1177 1541"> <thead> <tr> <th>Layer centre</th> <th><math>\sigma_1</math></th> <th><math>\sigma_{zz}</math></th> <th>Strain</th> <th>thickness</th> <th>disp</th> </tr> </thead> <tbody> <tr> <td>2</td> <td>32</td> <td>354</td> <td>0.0094</td> <td>4</td> <td>0.037</td> </tr> <tr> <td>7</td> <td>112</td> <td>102</td> <td>0.0024</td> <td>6</td> <td>0.015</td> </tr> <tr> <td>15</td> <td>240</td> <td>47.7</td> <td>0.0007</td> <td>10</td> <td>0.007</td> </tr> <tr> <td colspan="5" style="text-align: right;"><b>total=</b></td> <td><b>0.059m</b></td> </tr> </tbody> </table> Therefore 6 cm so acceptable.	Layer centre	$\sigma_1$	$\sigma_{zz}$	Strain	thickness	disp	2	32	354	0.0094	4	0.037	7	112	102	0.0024	6	0.015	15	240	47.7	0.0007	10	0.007	<b>total=</b>					<b>0.059m</b>	6 cm  Acceptable
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