

### VIII. Turbulence

#### A. review of where we've been

- laminar flow, rectilinear streamlines
- role of convection terms in momentum balance:
  - no convection across streamlines
  - convection terms along streamlines cancel
  - *no convection term in final balance equation*
- solutions apply for  $Re <$  some limit; what happens at large  $Re$ ?
- from here on, adios to non-Newtonian fluids

#### B. nature of turbulence

- *Mixing of momentum throughout the volume of fluid, which means that high momentum fluid and low momentum fluid are brought to the wall*
- *Transport of momentum to the wall.*

#### C. consequences of turbulence

- $\bar{v}$  fluctuates with time *fluctuates in time + space "chaotic"*
- significant fluctuations in  $\bar{v}$  across average streamlines:
  - convection of momentum across average streamlines:
  - *greatly increases rate of momentum transport to the wall.*
- must use time-average  $\bar{v}$  in equations  *$\langle v \rangle$  (might lose brackets later)*  
*"(and space)"*
  - time-average  $\bar{v}$  is nearly uniform across tube in tube flow
- *too complex for analytical solution*

#### D. results from dimensional analysis

Should be able to relate

$$\frac{\Delta P D}{\rho L \langle v \rangle^2}$$

$$\text{to } \frac{D \langle v \rangle \rho}{\mu}$$

formalize concept in "friction factors"