## Matlab Manual

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## 0 Matlab version

This manual describes (some) elements of Matlab Version 7.0 (or higher).

## 1 Matlab session

The way to start Matlab differs from computer to computer. You may type the command 'matlab' in a command window of the operating system. Often, though, you will have to click on a specific icon in order to run the program.

### 1.1 Getting started with Matlab

Once you have started Matlab a Matlab command window will appear, showing the command prompt:

```
% The Matlab command prompt.
```

The line after the prompt is called the command line. On this line you can give Matlab commands. After you have pressed <return>, Matlab will execute the command.

```
» pause(5) % Wait 5 seconds before showing the plot.
> plot (x,y) % Plot vector y versus vector x.
```

Besides the command window Matlab has graphical windows. Output of plot commands is directed to the graphical window.

The quit command enables you to leave Matlab. To terminate a running Matlab command you may use [Ctrl]+[c] (Press both the Ctrl button and the c button simultaneously).

By using the ! symbol you can use the original operating system

$$
\begin{array}{lll}
>!\text { printer command } & \% & \text { Execute the printer command belonging to the } \\
& \% & \text { original operating system. }
\end{array}
$$

Only for short computations it is useful to execute Matlab straightaway from the command line. In general the next procedure is much more practical:

1. Make a script file (see section 15) by means of your favorite text editor or the Matlab Editor/Debugger (see Section 1.3). A script file consists of a sequence of Matlab commands. In general script files will contain the main program and subprograms.
2. If necessary make the additional function files, using the same editor. Through these files we are able to define the functions which play a role in script files.
3. Matlab executes the commands in the script file after you have typed the name of the script file on the command line. Note, however, that the script file should be in the current (working) directory, indicated in the box above the command window.
From the command line background information can be obtained using

## 1. help

» help plot $\%$ gives information on the Matlab command plot.
2. demo
» demo $\% \quad$ presents multiple examples of the usage of Matlab.

### 1.2 Matlab and matrices, a general remark

Suppose that we define vectors $\mathrm{x}, \mathrm{y}$ and a matrix z by

$$
\begin{array}{ll}
x(i)=i & , i=1, \ldots, 10, \\
y(i)=i^{2} & , i=1, \ldots, 10, \\
z(i, j)=\sin (x(i) * y(j)) & , i, j=1, \ldots, 10 .
\end{array}
$$

In most programming languages a computer implementation will use nested loops:

```
» \(\boldsymbol{f o r} \boldsymbol{i}=1: 10\)
    \(x(i)=i ; y(i)=i^{\wedge} 2 ;\)
end
for \(i=1: 10\)
    for \(j=1: 10\)
        \(z(i, j)=\boldsymbol{\operatorname { s i n }}(x(i) * y(j)) ;\)
    end
end
```

In Matlab this can be done quite differently, because matrices are basic objects:

$$
\begin{aligned}
» x=1: 10 ; y=x . \wedge 2 ; z & =\sin \left(x .{ }^{*} y\right) ; \\
\% & \text { using a dot preceding the basic operation is vital } \\
\% & \text { here because all operations have to be taken elementwise, } \\
\% & \text { see also chapter } 8
\end{aligned}
$$

Both programming styles are possible in Matlab. However, the latter is far more efficient. Therefore we prefer the latter and all examples will be given in this style.

### 1.3 The Matlab Editor/Debugger

It is advantageous to use the Matlab Editor/Debugger when creating or editing script files. You invoke this editor by typing edit at the command prompt or from the File-New or FileOpen menu. The Matlab editor has various features to aid in editing script files so that most typing errors can be recognized. For example, text strings, reserved words (if, else, for, end, ...) and expressions are all shown in different colours. Saving and running the script is easily done using the Debug menu.

### 1.4 The Workspace Browser

The Workspace browser is invoked by the View-Workspace menu, giving a list of current variables (scalars, vectors, matrices), just as whos (Section 3) does. By double clicking on a
variable in the Workspace window the values of this variable are shown, in a separate window (the array editor), enabling inspection and interactive adaptations.

### 1.5 The property editor

Matlab directs graphical output to the graphical window. In this window the so-called property editor is available. Access is possible via the Edit or View button. Each graphical window contains several graphical objects such as axes and lines. One can select the different objects by clicking on them. Next, using the property editor one may inspect, make changes or add objects. This is in particular handsome in the final stage when it is needed to prepare the plot for inclusion in a report. It is the easy to add a title, label, etc.

## 2 Lay-out

When you use Matlab's default configuration, the program distinguishes upper case and lower case characters. One says that Matlab is case sensitive.

If the default configuration is used, Matlab will also print the result after every command. Typing ; (a semicolon) after the command will suppress this.

$$
\begin{aligned}
& \gg=2 \quad \% \quad \text { Matlab prints the result } \\
& x=\begin{array}{l} 
\\
2
\end{array} \\
& \gg=2 ; \quad \% \quad \text { Matlab does not print the result }
\end{aligned}
$$

The symbol $\%$ (comment) is used to give comments.

$$
\begin{array}{ccc}
\gg=2 & \% & \text { gives the value } 2 \text { to } x \text { and prints the result } \\
& \% & \text { printing the result can be suppressed with } ;
\end{array}
$$

The symbol ... (continuation) denotes that the command continues on the next line

$$
\begin{gathered}
>x=1+2+3+4+5+6+7+8+9+10 \ldots \\
+11+12+13+14+15+16+17+18+19+20 ; \\
\% \quad \text { this command does not fit on one line }
\end{gathered}
$$

## 3 Common Commands

| quit | $:$ | exit from Matlab |
| :--- | :--- | :--- |
| help command name | $:$ | gives information about a command |
| arrow up / down | $:$ | retrieves preceding and following commands |
| pause | $:$ | pauses execution, Matlab will proceed after <return> |
| whos | $:$ | gives a list of Matlab variables stored in the memory |
| clear | $:$ | clears the memory |
| clc | $:$ | clears the command window |
| clf | $:$ | clears the graphical window |
| shg | $:$ | closes the graphical window |
| close | $:$ | determines the elapsed cpu time |
| cputime | $:$ | activates Matlab demonstrations |

## 4 Numbers and strings

Numbers can be entered in Matlab in the usual way; however, spaces inside a number should be avoided.

$$
\begin{aligned}
& >(52 / 4-0.01) * 1 e-3 \\
& \text { ans }= \\
& \quad 1.2990 e-02
\end{aligned}
$$

Matlab automatically assigns a type for every number you enter. Depending on the type, Matlab chooses an internal representation for these numbers and the corresponding computations. The external representation of a number (e.g. on the screen) can be altered with the format command.

| format long e | 16 digits, (exponential) floating point $3.141592653589793 \mathrm{e}-02$ |  |
| :---: | :---: | :---: |
| format shorte | 5 digits, (exponential) floating point | 3.1416e-02 |
| format short | 5 digits, fixed point | 0.0314 |
| format long | 15 digits, fixed point | 0.03141592653590 |
| format | returns to the default configuration |  |

The default configuration is 'format short'. It might be possible that the local system manager has changed this into short e.

Remark: The format command influences only the external representation of real numbers. This command has no influence on the internal representation used by Matlab to process the program and its computations.

Remark: The format command is not able to alter the external representation of integer numbers. This can result for example in jumps in tables.

The command vpa from the Symbolic Toolbox is helpful for displaying numbers and variables:

$$
\begin{aligned}
& \gg=\mathbf{x i} / 10000 ; \mathrm{d}=8 ; \boldsymbol{\operatorname { d i s p }}(\mathbf{v p a}(\mathrm{x}, \mathrm{~d})) \\
& .31415927 \mathrm{e}-3
\end{aligned}
$$

In the above the variable d in the call of vpa refers to the number of digits to be displayed.
To manipulate text, Matlab uses strings.
» disp ('give the spring constant $a^{\prime}$ )
give the spring constant a

## 5 Variables

A variable's name has to start with a letter, but may not contain more than 31 letters, digits, or underscores. Matlab is case sensitive in its default settings. This means that j and J do not have the same meaning. Matlab automatically reserves space in the computer's memory to store the variable. Variables do not need to be declared before use; Matlab derives the type of the variables by looking at the stored data. So it is possible that the type of a variable changes while a session is in progress.

The basic element of Matlab is the matrix. Depending on the size of the matrix we distinguish scalars ( $1 \times 1-$ matrix ), vectors ( $1 \times \mathrm{m}-$, or $\mathrm{m} \times 1-$ matrix), etc. Depending on the context Matlab also assigns the type of the variables in the matrix, e.g. real or complex.

The operators $+,-,{ }^{*}, /, \wedge$ can be used for all Matlab variables $\left(x^{\wedge} y=x\right.$ to the power of $\left.y\right)$. In the scalar case these operations will reduce to the usual computations. At every operation step Matlab checks if the dimensions of the matrices involved are correct.
$» a=1 ; c=1+i ; v(1)=1 ; v(2)=2 ;$ word $=$ 'text';
The command whos (see section 3) gives:

| Name | Size | Class |
| :---: | :--- | :--- |
| a | $1 \times 1$ | double array |
| c | $1 \times 1$ | double array (complex) |
| v | $1 \times 2$ | double array |
| word | $1 \times 4$ | char array |

Multiplying a vector v with itself is not possible. If we try this anyhow we get:
$\gg=v * v ;$
??? Error using ==» *
Inner matrix dimensions must agree.

## 6 Complex variables

A complex number can be defined using the imaginary number i .

$$
\begin{aligned}
& \gg=1+\mathbf{i} \\
& c= \\
& \quad 1.0000+1.0000 \mathbf{i}
\end{aligned}
$$

The operators $+,-,{ }^{*}, /, \wedge$ also work for complex numbers. With the symbol ' we conjugate a complex variable:

$$
\begin{aligned}
& >\text { cgec }=c^{\prime} \\
& \text { cgec }= \\
& 1.0000-1.0000 \mathbf{i}
\end{aligned}
$$

The (square of the) modulus of c can be computed in the following way:

$$
\gg \bmod c 2=c^{\prime} * c
$$

$$
\begin{aligned}
& \bmod c 2= \\
& 2.0000
\end{aligned}
$$

An alternative method is:

$$
\begin{gathered}
>\bmod c 2=\boldsymbol{a b s}(c)^{\wedge} 2 \\
\operatorname{modc} 2= \\
2.0000
\end{gathered}
$$

Imaginary and real parts of a variable can be obtained with the functions real and imag:

```
\(\gg a=\) real (c)
\(a=\)
    1.0000
\(\gg b=\boldsymbol{i m a g}(c)\)
\(b=\)
    1.0000
```


## 7 Matrices and Vectors

Matlab stores its variables in matrices of size n x m . If $\mathrm{m}=1$, we are dealing with a column vector, and if $\mathrm{n}=1$, with a row vector. When $\mathrm{n}=\mathrm{m}=1$ the matrix represents a scalar. The size of a matrix does not have to be given; Matlab determines the size from the data given by the user. Matlab does not recognize a more general array structure, for example v (-10:100); the lower bound in Matlab is always equal to 1 .

We can define matrices in different ways, e.g. by giving values to every element separately. We separate row entries by a space or comma and column entries by a semicolon or a <return>.

```
> A=[ll 2 3;4,5,6;7 8 9] % generating matrix A
    A=
        1 2 3
        4 5
        7 8 9
> A = [1 2 ...
            34;
            5678] % generating matrix A; ... means continuation
        A =
        1234
        5678
```

Vectors can also be made using the colon symbol : . Here the first value stands for the initial value, the second for the step size.

\[

\]

The default vector in Matlab is a row vector as can be seen here. If a column vector is needed, extra measures are needed (see later on).

Sometimes it is good to use one of the following Matlab functions:

```
zeros(n,m) : gives an n x m matrix with zeros
ones(n,m) : gives an n x m matrix with ones
eye(n) : gives the n x n identity matrix
>A = ones(3,3) + 2*eye(3) % generating matrix A
    A =
    311
```

$$
\begin{array}{lll}
1 & 3 & 1 \\
1 & 1 & 3
\end{array}
$$

Matrices can also be built from smaller variables

$$
\begin{aligned}
& \gg v=\text { ones }(3,1) ; A=[-v 2 * v-v] \quad \% \quad \text { generating matrix } A \\
& A= \\
& -1
\end{aligned}
$$

Sometimes it is useful to contruct matrices by concatenation.

$$
\begin{aligned}
& » \quad v 1=\left[\begin{array}{ll}
1 & 2
\end{array}\right] ; v 2=\left[\begin{array}{ll}
3 & 4
\end{array}\right] \text {; } \\
& \gg \quad v=\left[\begin{array}{ll}
v 1 & v 2
\end{array}\right] \quad \text { o or } v=\boldsymbol{c a t}(v 1, v 2) \\
& v= \\
& \begin{array}{llll}
1 & 2 & 3 & 4
\end{array} \\
& \gg E=\operatorname{eye}(3) ; C=\operatorname{zeros}(3,2) ; D=[E C] \\
& D= \\
& 10000 \\
& 01000 \\
& 00100
\end{aligned}
$$

Large diagonal band matrices can be made by using the function

$$
\begin{aligned}
& \operatorname{diag}(\mathrm{v}, \mathrm{k}): \quad \text { returns a square matrix with on the } \mathrm{k} \text {-th upper diagonal the entries } \\
& \text { of the vector } v \text {. } \\
& » v=1: 2: 9 \quad \% \quad \text { generating vector } v \\
& v= \\
& \begin{array}{lllll}
1 & 3 & 5 & 7 & 9
\end{array} \\
& » A=\operatorname{diag}(v,-1)+\boldsymbol{e y e}(6)+2 * \operatorname{diag}(v, 1) \\
& A=
\end{aligned}
$$

Matrix elements can be used separately or in groups:

```
\(\mathrm{A}(\mathrm{i}, \mathrm{j}) \quad=\quad \mathrm{A}_{\mathrm{ij}}\)
\(A(:, j) \quad=\quad j^{\text {th }}\) column of A
\(\mathrm{A}(\mathrm{i},:) \quad=\quad \mathrm{i}^{\text {th }}\) row of A
\(A(i, j 1: j 2)=\) vector existing of the entries, from column j 1 to j 2 , of row i
\(A(i 1: i 2, j 1: j 2)=\) matrix existing of the entries, from column \(j 1\) to \(j 2\), of the
    rows i1 to i2.
》 \(x=A(2,3)\)
    \(x=\)
        6
» plot ( \(x\) (75:125) , y(325:375) );
```

In case one of the dimensions equals one we are dealing with a vector．We can refer to this vector with just one index．This index is either a row index or a column index，depending on the type of the vector．

Note：
Matrix elements can also be addressed using one index only．This might sometimes be handy． One－dimensional references are taken column wise by Matlab：

$$
\begin{aligned}
& » A=[123 ; 456 ; 789] ; \\
& \text { 》 } x=A(6) \\
& x= \\
& 8
\end{aligned}
$$

However，in many cases such a reference is the result of a programming error，and then one must be aware of the fact no error message will be given．

## 8 Matrix and array operations

Arithmetic operations on matrices and vectors come in two distinct forms. Matrix sense operations are based on the normal rules of linear algebra and are obtained with the usual symbols +, -, *, /, ^. Array sense operations are defined to act elementwise and are obtained by preceding the symbol with a dot.

$$
\begin{array}{lll}
>v=v 1 . * v 2 ; & \begin{array}{c}
\% \\
\%
\end{array} & \begin{array}{l}
\text { multiply } v 1 \text { and } v 2 \text { element by element } \\
v(1)=v 1(1)^{*} v 2(1), \ldots ., v(n)=v 1(n) * v 2(n) .
\end{array} \\
>y=v . \wedge 2 ; & \% & y(1)=v(1)^{\wedge} 2, \ldots, y(n)=v(n)^{\wedge} 2 .
\end{array}
$$

A very useful extra matrix operation is presented by taking the transpose

```
» B=A'; % transpose A
» B=transpose(A); % alternatively
```

In the case of matrix operations linear algebra introduces restriction with respect to the dimensions of the matrices involved. Of course, Matlab checks for this.

```
»v(1)=1;v(2)=2;v(3)=3;A=\boldsymbol{eye}(3);% A is the 3x3 identity matrix.
> w = A * v;
??? Error using ==» *
Inner matrix dimensions must agree.
```

Matlab assumes that the index of every new vector is a column index, i.e. unless explicitly specified otherwise (see example below), the new vector is a row vector. Hence in the example above v is a row vector, which results in an error message.

```
>v=\boldsymbol{zeros}(3,1); % v is forced to be a column vector
»v(1)=1;v(2)=2;v(3)=3;A=\boldsymbol{eye (3);}
>w = A*v;
>v(1)=1;v(2)=2;v(3)=3;A=\boldsymbol{eye}(3);
>v=v'; % change v into a column vector
> w = A*v;
 inprod = v'*v % inner product if v is a column vector.
```


## 9 Elementary mathematical functions and constants

Some of the predefined constants in Matlab are:

| $\mathbf{p i}$ | $:$ the constant pi |
| :--- | :--- |
| $\mathbf{i}$ | $:$ the imaginary unit |
| inf | $:$ infinity |

The following mathematical functions operate in array sense, i.e. on each element of the variable separately:

| abs | $:$ absolute value or modulus (complex case) |
| :--- | :--- |
| sqrt | $:$ square root |
| exp | $:$ exponential function |
| $\mathbf{l o g}$ | $:$ natural logarithm |
| $\boldsymbol{\operatorname { l o g } 1 0}$ | $:$ logarithm with base 10 |
| $\mathbf{\operatorname { s i n }}$ | $:$ sine |
| $\mathbf{c o s}$ | $:$ cosine |
| $\boldsymbol{\operatorname { t a n }}$ | $:$ tangent |
| $\boldsymbol{\operatorname { a t a n }}$ | $:$ arctangent |
| round | $:$ round off to the nearest integer |
| rem | $:$ remainder after division |

For vectors are available:

```
max(v) : maximal element of the vector v
min(v) : minimal element of the vector v
sum(v) : sum of the elements of the vector v
length(v) : returns the size of the v
norm(v) : returns the Euclidean norm of the vector v,
    i.e. norm(v)=sqrt(sum(v.^2)).
norm(v,inf) : returns the infinity norm of the vector v,
    i.e. norm(v)=max(ads(v)).
> max(abs(v)) % computing the largest element of v, irrespective of its sign
```

For matrices we mention

| size(A) | returns the transpose of a matrix <br> returns the size of a matrix |
| :---: | :---: |
| $\operatorname{det}(\mathrm{A})$ | : returns the determinat of a matrix |
| transpose(A) | returns the transpose of a matrix |
| $\mathbf{e i g}(\mathrm{A})$ | : determines the eigenvalues (and eigenvectors) of the matrix A |
| $\mathbf{l u}(\mathrm{A})$ | determines the LU-factorization of the matrix A (using permutations if necessary). |
| chol(A) | determines the Cholesky factorization of a symmetric matrix |

## 10 Conditional statements

A conditional statement is a command that allows Matlab to take a decision of whether to execute a group of commands that follow the conditional statement, or to skip these commands. In a conditional statement a conditional expression or condition is stated. If the condition is true, a group of commands that follow the statement is executed.

## The if-end structure

if condition
commands
end

## The if-else-end structure

if condition
commands [1]
else
commands [2]
end

## The if-elseif-else-end structure

if condition
commands [1]
elseif condition
commands [2]
else
commands [3]
end
The condition needs to be a relational or logical expression taking the value true or false, in Matlab 1 (true) or 0 (false).

In Matlab six relational operators can be used to compare variables or evaluate expressions

$$
\begin{array}{lll}
< & : & \text { smaller than } \\
<= & : & \text { smaller than, or equal to } \\
> & : & \text { greater than } \\
>= & : & \text { greater than, or equal to } \\
== & : & \text { equal to } \\
\sim= & : & \text { not equal to } \\
>x=5 ; y=10 ; x<y \\
& \quad \% \quad \text { thus true }
\end{array}
$$

Furthermore there are three basic logical operators:

```
& : and
| : or
~ : not
> x=5;y=10;x>1 & y<==5
    0 % thusfalse
```

Combining all of this one may see:

An example:

```
> if \((x>=1 \& y>=1)\)
    \(a=1\);
elseif \(\sim(x>=1) \& \sim(y>=1)\)
    \(a=-1 ; \quad \% \quad\) both \(x\) and \(y\) less than 1
    else
    \(a=0 ; \quad \% \quad\) either \(x\) or \(y\) less than 1
    end
```


## 11 Loop Statements

## FOR - loop

Syntax:
for variable $=$ start value : increment $:$ end value commands
end
The increment can be positive as well as negative. If not defined, Matlab will use increment 1 as a default.

$$
\begin{aligned}
& \text { » } \boldsymbol{f o r} j=0: 10 \\
& v(j+1)=j * 0.1 ; \% \quad \text { the row vector } v \text { needs to start at index one! } \\
& \text { end }
\end{aligned}
$$

## WHILE - loop

Syntax:
while condition
commands
end
The condition needs to be a relational or logical expression.

```
> x = 1;
> while ( }x>10^-6
    x = x/2;
    end
```


## Forced exit from loops

A loop can be terminated with the break statement, which passes control to the first statement after the corresponding end. This is in particular handsome to avoid infinite while-loops, because sometimes it is not certain that the condition will be met at a certain moment.

| tol $=10^{\wedge}-6 ;$ | $\%$ | specify tolerance <br> criterium $=$ inf; <br> $m=0 ;$ |
| :--- | :--- | :--- |
| while criterium $>$ tol | $\%$ | initialize to a large number <br> initialize counter to zero |
| compute a new approximation $x$ |  |  |
| compute an updated value of criterium for this $x$ |  |  |
| $m=m+1 ;$ | $\%$ | count |
| if $m>1000$, break, end | $\%$ | jump out if too many |
| end |  |  |

This example presents a typical implementation of a numerical iterative procedure to obtain a numerical approximation within a specified tolerance taking into account that the numerical procedure might not converge.
Influence of round-off

```
> x = 0;
>while (x<1)
        x = x+0.1;
    end
> }
x=
    1.1000
```

Note that this is not a proper method when we want to execute the loop statement exactly ten times. In Matlab 10 times 0.1 is just a bit less then 1, because Matlab makes round-off errors. This means that the loop will be executed 11 times in stead of 10 times, and therefore the final value of x will be too big. In such a case it is better to rely upon integer computation.

```
» \(x=0\);
》 \(\boldsymbol{f o r} j=1: 10\)
    \(x=x+0.1 ;\)
    end
```

In order to force integer computation the command round (section 9) is often useful.

## 12 Output

Output can be directed to the screen with the command disp.

| $\operatorname{disp}(\mathrm{x})$ | $:$ | print the value of the variable x |
| :--- | :--- | :--- |
| $\boldsymbol{\operatorname { d i s p }}($ 'text') | $:$ | print the string 'text' |
| $\boldsymbol{\operatorname { d i s p } ( \mathrm { A } ( : 5 ) )}$ | $:$ | print the 5-th column of matrix A |

With the command format or vpa we can define how a number is displayed (see section 4).
Remark: Advanced control mechanisms for printing are available with the command fprintf. (see the example program in section 19 or use help fprintf)

We can write data to a file.
\(\left.$$
\begin{array}{lll}\text { save data varlist } & : \begin{array}{l}\text { the variables in varlist are written to the file } \\
\text { data.mat in binary format. This file can be used in } \\
\text { a subsequent session. }\end{array}
$$ <br>
the variables in varlist are written legible (8 <br>

digits, floating point) to the file output. If\end{array}\right]\)| necessary this file can be printed. |
| :--- |
| makes a diary of everything which happens |
| during the session and writes this to the file |
| output. If necessary this file can be printed. |
| stops monitoring the session. |

$\gg x=0: 0.1: 1 ; y=\exp (x) ;$ table $=\left[x^{\prime} y^{\prime}\right]$
» format compact $\%$ suppress empty lines in output
» diary output $\%$ open the file output as output file
$» \operatorname{disp}\left(\begin{array}{ll}x & y\end{array}\right) \quad \% \quad$ display the header of the table
» disp (table); $\%$ display a table containing $x$ and $y$
» diary off
The fifth line uses Matlab matrix features. Alternativily, one may use the more classical:

```
» \(\boldsymbol{f o r} j=1: 10\)
    \(\operatorname{disp}([x(j), y(j)]) \% \quad\) display the values
    end
```

Remark: The diary command easily gives an unnecessary amount of output. Therefore: Use the diary command in a selective way and only at places where output is needed.

Remark: $\quad$ Files can be printed using the printer command of the original operating system, see section 1 .

Remark: Depending on the operating system other printer commands might be available. Be careful in using these commands, because they can cause an unnecessarily long waiting time for other people who want to use the printer. Using the printer command (in the file menu) you can print the whole Matlab session.

## 13 Input

Variables can be entered in Matlab in different ways. The first method is using the command line. We already explained how to do this. Another way to enter it is:
$» x=$ input (' $x$-coordinate $=$ ');
This command writes the text from the string to the screen, waits for input (until a <return> is given) and assigns the value given by the user to the variable x . The following command:
» load data
fetches the binary file data.mat. The file data.mat needs to be produced beforehand in Matlab and besides a list of variables it also contains the values of these variables.

The command
» load data.txt
fetches an ASCII file with the name data.txt. The content is stored in a double precision array with the name data. The file data.txt is only allowed to contain numbers, separated by blanks. Each line of the file corresponds with a row in the array data. Each number on a line corresponds with a column in the array data. The number of columns must be equal on each line.

### 13.1 The import wizard

Data can also be imported using a graphical user interface, called the Import Wizard. Choose in the File menu the option Import Data to start the Import Wizard. Then choose a file in the new window from which data should be read, preview the data, and if you are satisfied, use the next and finish buttons to import the variables in the Matlab workspace. You may check the imported variables afterwards, using whos (Section 3) or the Workspace Browser (Section 1.4).

## 14 Graphical Output

General commands affecting the graphical screen are:

| clf | $:$ | clear graphical window <br> show graphical screen (bring graphical screen to the <br> foreground) |
| :--- | :--- | :--- |
| shg | $:$ | close the graphical window <br> keep the contents of the graphical screen during new plot <br> commands |
| close | $:$erase the contents of the graphical screen before executing <br> now on |  |
| hold off | $:$ | direct the graph to the printer <br> store the graph in the file 'filename' |
| print |  |  |

Commands affecting the layout of the graph are:

```
linspace(x1,x2,n) : generates a grid of n points on [x1,x2]
axis ([xmin xmax ymin ymax] ) : sets the axes according to the given values
grid : adds a grid to the graph
title('text') : writes text above the plot
xlabel('text') : writes text underneath de x-axis
ylabel('text') : writes text next to the y-axis
text(x,y,'text') : writes text at the point (x,y) of the graphical
    screen
t= num2str(var) : makes text of the value of var, which can
    for example be written to the screen with
    text(x,y,t).
```

Some basic graphical commands are:

| linspace( $\mathrm{x} 1, \mathrm{x} 2, \mathrm{n}$ ) | generate a grid of n points on [ $\mathrm{x} 1, \mathrm{x} 2$ ] |
| :---: | :---: |
| plot (y) | plots the vector y versus the indices $1, \ldots, \mathrm{n}$. |
| plot (x,y) | plots the vector y versus the vector x ; x and y must be of the same size. |
| plot (x,y, 'symbol') | plots the vector y versus the vector x by using a symbol or color, e.g. ':' (dotted), '-' (dashed), 'o' (circles), 'x ' (crosses), 'y ' (yellow line), ' $r$ ' (red line), ' $g$ ' (green line) |
| fplot (@f,[xbegin xend]) | plots the function $f$ on the interval [xbegin, xend]. |
| plot ([xbegin xend],[ybegin yend]) | draws a line from (xbegin, ybegin) to (xend, yend). |
| zoom | makes it possible to zoom in at a specific point in the graph by clicking at that point. |
| ginput(n) | gets the coordinates of $n$ points in the graph, which are located by positioning the |

cursor and thereupon clicking the mouse.
Remark: help plot shows all the possible arguments with plot.

```
>x=[0:20]/10; y = \boldsymbol{sin}(\boldsymbol{pi*}*);
>plot (x,y); % plot sin \pix on [0,2], plot
    % automatically assigns the right limits
    % to the axes in the graphical screen.
»\boldsymbol{axis ([[0 [ 2-1 1}])\mathrm{ ); % adjust the x-axis and the y-axis; it is}
    % preferable to call axis after plot
» xlabel ('x'); ylabel ('sin x');
print % send the graph to the printer.
> clf
> hold on
» type = ['- ' ; ': ; '- .' ; '- -'] }\begin{array}{l}{%}\\{%}\end{array}\begin{array}{l}{\mathrm{ spaces to equalize the length of the}}\\{\mathrm{ character strings }}
> xgraph = [0:100]/100;
>for j=1:4
        omega =j *pi; % plotsin(\omegax) on [0,1]
        ygraph = sin (omega * xgraph); % for }\omega=\pi,2\pi,3\pi,4\pi
        plot (xgraph,ygraph,type(j,:));
    end
> print figure
    % distinguish the curves visually
```

$\% \quad$ for $\omega=\pi, 2 \pi, 3 \pi, 4 \pi$,
$\%$ distinguish the curves visually
\% store the graph in a file named figure;
$\% \quad$ use help print to see a list of
\% available formats.

Some commands for 3 dimensional graphs are:

```
plot3(x,y,z) : plots a line through the coordinates of vectors x, y, z.
\operatorname{surf}(x,y,Z) : plots the matrix Z versus the vectors y and x, creating a
    surface.
\operatorname{surfc}(x,y,Z) : same as surf, but adds a contour plot beneath the surface.
mesh(x,y,Z) : plots the matrix Z versus the vectors y and x, creating
    a surface together with a mesh on it.
meshgrid(x,y) : creates matrices for a 2D product grid from two 1D vectors.
rotate3d : enables the user to rotate the plot by mouse.
```

```
>t=[0:500] * pi/50;
> x=\boldsymbol{\operatorname{sin}}(t);y=\boldsymbol{\operatorname{cos}}(t);
> x = [0:10] / 10;
> y = [0:20] / 10;
»[X,Y]=meshgrid}(x,y
» Z=sin(X+Y);
>mesh(X,Y,Z); % or surf(X,Y,Z)
```

» $\boldsymbol{p l o t} 3(x, y, t) \quad \%$ plots a spiral on the cylinder
$\% \quad x^{2}+y^{2}=1$.
\% build a 2D product grid by
$\begin{array}{ll}\% & \text { build a } 2 D \text { pro } \\ \% & \text { forming } x \otimes y \\ \% & \text { compute }\end{array}$
$\% \quad$ compute function values on the grid
\% plot $\sin (x+y)$ for $x=0: 0.1: 1$

Moreover, Matlab has some easy to use plotting routines with names starting with ez. Examples are:

| ezplot | $:$ | plots a function $f(x)$ on an interval |
| :--- | :--- | :--- |
| ezsurf | $:$ | presents a surface of a function $f(x, y)$ |

As has been mentioned in section 1.5, the property editor can be used conveniently to manipulate the graphical window.

## 15 Script files, function files

### 15.1Script files

A script file is a file that consists of a sequence of Matlab commands: a Matlab program. We make such a file with the help of the Editor. The standard extension for these files is .m, e.g. program.m. The commands in the script file are executed after the filename is typed on the command line (without extension .m, i.e. in the example above you need to type 'program'). It is also possible to run a script file from another Matlab program (see section 20).

```
% plotsin.m : The script file creates a plot of
%}\quad\mathrm{ the function sin(x) on the interval [0, }\pi
clear; clc; clf; % clear
x= linspace(0, pi,41);% create a grid with spacing \pi/40 on [0, \pi].
y = \boldsymbol{\operatorname{sin}}(x);
plot(x,y);
axis([0 pi-1 1]); % set limits along axes
title('sin(x)'); % put text above the plot
```


### 15.2Function files

By means of function files we can add new functions to Matlab. A function file contains a sequence of commands, like a script file, but by means of input and output variables it is possible to communicate with other files. The filename of a function file is used to execute the function.

A function file has the following form:
function output_variable = function_name(input_variable) commands

The word function on the first line implies that it is a function file and not a script file.
Remark: At the position of function_name you need to fill in your chosen name for the function. The filename of the file containing this function must be the same as this name with the standard extention .m. Similar to names of variables, the function name is not allowed to start with a number.

Both the input variable as well as the output variable may be matrices or vectors.

```
function \(y=\operatorname{average}(v)\);
\(\%\) This function computes the average of the elements of vector \(v\).
\(\%\) The function is stored in the file average.m
```

$$
\begin{aligned}
& n=\operatorname{length}(v) ; \\
& y=\operatorname{sum}(v) / n ;
\end{aligned}
$$

Having defined the function average, stored in the file average.m, this function is available for scripts and other functions.
\% examplescript.m : script file to compute average temperature

```
T = [ll7.0 18.5 17.8 17.9 18.3];
averT = average(T);
disp(averT);
```


### 15.3Collecting multiple Matlab files

Matlab does not allow for a mixture of scripts and functions in a single file. However, functions and subfunctions can be collected in a single file. As an example we present a single file, called examplescript.m, containing both files from subsection 15.2.

```
function examplescript
% EXAMPLESCRIPT This function executes the commands as contained in the
%
% and output arguments are used.
```

```
T = [17.0 18.5 17.8 17.9 18.3];
```

T = [17.0 18.5 17.8 17.9 18.3];
averT = average(T);
averT = average(T);
disp(averT);
disp(averT);
function y = average(v);
function y = average(v);
% This function computes the average of the elements of vector v.
% This function computes the average of the elements of vector v.
n= length(v);
n= length(v);
y=\boldsymbol{\operatorname{sum}}(v)/n;

```
y=\boldsymbol{\operatorname{sum}}(v)/n;
```

Typing examplescript on the command line, excutes the script. However, it is a disadvantage that the workspace can not be accessed easily using the Workspace Browser because functions have local workspaces.

### 15.4 Parameters and Functions

Functions and subfunctions have local memories and, as a consequence, variables used in the function file are local (i.e. only accessible inside the function), and therefore they are not stored in and/or taken from the central Matlab memory.

$$
\text { function } y=\operatorname{comp}(x) \text {; }
$$

$y=a * x ; \quad \% \quad$ the variable a is defined locally and does not
\% have a value irrespective of the outside world,
$\% \quad$ i.e. an error message follows
function $y=\operatorname{comp}(x)$;

$$
\begin{array}{lll}
a=2 ; & \text { \% } & \text { the variable a has the value 2, only within this } \\
y=a * x ; & \% & \text { function and this value is not know elsewhere. }
\end{array}
$$

Often it is neccessary to use a parameter in a function that gets its value outside the function. You can show Matlab you want to use such a parameter by adding it to the list of that function. In the following example we add the variable a to the list of the function comp:

```
function \(y=\operatorname{comp}(x, a)\);
\(y=a * x ; \quad \% \quad\) the variable a gets its value outside the function
    \(\%\) and is passed to the function
```

This is not always possible. It may sometimes be necessary to define a variable globally, by using global. If you do so the variable is defined in all program parts that contain the same global declaration.

```
function \(y=\operatorname{comp}(x)\);
global \(a\);
\(y=a * x ; \quad \% \quad\) the variable a must also be defined globally
    \% at other locations, i.e. specifically
    \(\% \quad\) where a gets its value.
```

Remark: The declaration with global should only be used when there is no other possibility. If you use it, it is wise to add some comments.
Remark: In the context of the courses for which this manual is written a convenient way to communicate parameters, avoiding the global command, is to use nested functions, see subsection 19.2.

For an example of the use of global see subsection 19.1.

## 16 Solving a system of equations

To solve systems of equations $\mathrm{Ax}=\mathrm{b}$ we can use several methods:
i) If a small system with a full matrix needs to be solved only once, we may use the black box option:

$$
\gg x=A \mid b ;
$$

Often it is necessary to be more specific to obtain an efficient program. As an example we mention:
ii) If more than one system needs to be solved with the same matrix $A$, but different righthand sides:

$$
\begin{array}{lll}
\gg L L, U]=\boldsymbol{l} \mathbf{u}(A) ; & \% & \text { Make an LU-decomposition of } A \\
>y=L \backslash b ; & \% & \text { Solve lower triangular system } \\
\gg x=U \backslash y ; & \% & \text { Solve upper triangular system } \\
\gg y 2=L|b 2 ; x 2=U| y 2 ; & \% & \text { Solution for other right-hand side }
\end{array}
$$

iii) If the matrix is symmetric and positive definite, we may use the Cholesky decomposition:

$$
\begin{array}{lll}
\gg=\operatorname{chol}(A) ; & \% & \text { Make a Cholesky decomposition of } A: R^{\prime} R=A \\
>y=R^{\prime} \mid b ; & \% & \text { Solve lower triangular system } \\
\gg x=R \mid y ; & \% & \text { Solve upper triangular system }
\end{array}
$$

In all cases the command $\mathrm{A}=\boldsymbol{\operatorname { s p a r s e }}(\mathrm{A})$ can save a lot of runtime and memory space when A is a band matrix. As an example we give the number of floating-point operations for the case where A is a symmetric tridiagonal matrix of size $100 \times 100$.

|  | without sparse(A) | with sparse(A) |
| :--- | :---: | :---: |
| method i | 378350 | 2149 |
| method ii | 35250 | 1889 |
| method iii | 358750 | 1393 |

## 17 Tracking down errors

Matlab does not give specific directions for debugging programs. In any way it is useful to generate (intermediate) output, and if necessary to recalculate it manually. Some useful commands are:


The Workspace Browser (Section 1.4) provides a very simple, but often effective, way to check names, types and sizes of variables. Moreover, variables can be opened in the array editor and then it is easy to check the values of the variables in use.

A more advanced feature can be found in the Matlab editor. After opening a Matlab file one can use the Debug menu, and, among others, set breakpoints.

## 18 Symbolic Computing

Matlab offers the Symbolic Math Toolbox, which is based upon the Maple kernel from Waterloo Maple, inc. This Toolbox allows symbolic manipulation of variables in a way very much similar to Maple, so it might be helpful to consult your Maple Manual. To obtain an overview of functions in the toolbox type help symbolic in the Matlab window. A short survey is given below.

```
symx : declare x to be a symbolic variable
syms x y : declare x and y to be symbolic
subs(y,x,value) : substitute the 'value' for x into the symbolic expression y
```

As an example, observe the effect of following commands

```
» syms x y % declare x, y to be symbolic
>y=sqrt(x)
>yl=\boldsymbol{subs}(y,x,2)\quad%\quad\mathrm{ substitute }x=2\mathrm{ into }y=\sqrt{}{\textrm{x}}
y2=\boldsymbol{subs}(y,x,\operatorname{sym}(2))\quad%\quady2 will be symbolic
>yv=subs(y,x,1:10) % yv will be a vector
```

Expressions may contain several symbolic objects which can be substituted by a call to subs with lists (so-called cell arrays in Matlab) as second and third argument. Symbolic integration and differentiation is performed through the int and diff functions, as in Maple. The resulting expression sometimes appears to be quite complicated; then simplify, factor or conversion to numeric form, using double might help.

```
diff(f,x) : differentiate f with respect to x
int(f,x,a,b) : integrate f with respect to x from a to b
simplify(y) : simplify the symbolic expression y
factor(y) : factorize the symbolic expression y
double(y) : convert the symbolic expression into a
    floating point number
>Syms x y
>f=sqrt(1+x^2+\mp@subsup{y}{}{\wedge}2)
>f12=subs(f,{x,y},{1,2}) % substitute }x=1\mathrm{ and }y=2\mathrm{ into f
>f12num=double(f12) % convert f12 to floating point
>fx=\operatorname{diff}(f,x)\quad% differentiate w.r.t. x
>fxsim=simplify(fx) % simplify
```

Expressions can be solved for a variable using solve, whereas dsolve tries to solve differential equations symbolically. The derivatives are denoted by D, D2, etc., and initial conditions can be passed as additional arguments.

```
solve (f,x) : solve f=0 for x
dsolve(deq,init) : solve the differential equation given by deq
    for the initial value init
```

>Syms $x$ ac
$\gg f=a^{*} x^{\wedge} 2+c$
$>x 0=\operatorname{solve}(f, x) \quad \%$ find the zeros off
$\gg 0=$ solve ( $' a * x+c=0$ ') $\quad \%$ solve $a x+c=0$
$\gg=$ dsolve( $D 2 x+x=0$ ') $\quad \% \quad$ solve the differential equation $x$ '" $+x=0$
$\gg=$ dsolve ( $' D 2 x+x=0$ ', ' $x(0)=1$ ') $\%$ solve the differential equation with initial
$\% \quad$ value $x(0)=1$

## 19 Functions, some advanced issues

Function files, often userdefined, form the heart of Matlab applications. In this section we pay attention to some advanced features related to communication.

### 19.1 Passing a function as an argument

A function can be passed as an argument by using a function handle or an anonymous/inline object or a string. We recommend the usage of function handles and/or anonymous objects (the two are closely related).

$$
\begin{array}{ll}
\% & \text { program.m: } \\
\%
\end{array} \quad \begin{aligned}
& \text { script file to plot the function } f(x)=x^{\wedge} m ; \\
& \text { uses the function file f.m }
\end{aligned}
$$

global m;
$m=2$;
fplot(@f,[0,1]); \% @ is the function handle
The function $f$ is given in the following function file:

$$
\begin{array}{lll}
\begin{array}{l}
\% \\
\text { f.m }
\end{array} & : & \text { Function file presenting the function } x \wedge m: \\
\text { function fvalues }=f(x) ; & & \\
\text { global } m ; \\
\text { fvalues }=x . \wedge m ; & \% & \text { note the usage of array operations } \\
& \% & \text { the function fis called with an } \\
& \% & \text { array as input variable. This } \\
& \% & \text { array contains multiple } x \text {-values. }
\end{array}
$$

Remark: The usage of global is not really necessary, as the routine fplot could be called differently, see subsection 19.2.

### 19.2 Communicating parameters

In the context of the courses for which this manual is written it is often needed to vary parameters which are present in low-level routines. We can communicate parameters using the global command. However, this is not recommended. There are several alternatives of which we mention the two we like most:

- use nested functions
- use command line functions in the form of anonymous functions

The first method is advocated in some text books. The second method is frequently mentioned in the Matlab help.

In order to focus, we consider the initial value problem

$$
\left\{\begin{array}{l}
\frac{d y}{d t}=-a y+\sin t . \\
y(0)=1
\end{array}\right.
$$

The parameter a needs to get its value outside the function file presenting the right-hand side of the differential equation. In the examples below we use the Matlab routine ode45 for the numerical integration of the differential equation. If needed, it is easy to substitute your own solver, either as a stand-alone routine or as a nested function.

## Nested functions

The underlying mechanism for communication of parameters is that nested functions share the same workspace. This enables easy communication of parameters. If functions are nested, then it is obligatory to use end on the last line of the function

```
function solvede % level 0
% SOLVEDE solves a simple DE % top level
a=2; }\quad%\mathrm{ give a its value at the top level
y0=1; tspan=[0 1];
[t,y]=ode45(@ownrhs,tspan,y0); % function handle
plot(t,y);
    function fvalue = ownrhs(t,y) % level 1
    % OWNRHS contains the user-supplied rhs of the DE
    % ownrhs shares the workspace of solvede and thus
    % it is possible to use the parameter a freely
    fvalue = -a* * y sin(t);
    end % end of ownrhs
end % end of solvede
```


## Anonymous functions

The above example can be done on basis of a script file solvede and a separate function file ownrhs.
$\%$ solvede.m : script file to solve a simple $D E$
$a=2 ;$
$y 0=1 ;$ tspan $=\left[\begin{array}{ll}0 & 1\end{array}\right]$;
fhandle $=@(t, y)$ ownrhs $(t, y, a) ; \quad \%$ function handle, presenting both the \% basic variables as well as the \% parameter
[t, y] = ode45(fhandle, tspan, y0);
$\boldsymbol{p l o t}(t, y)$
The anonymous command line function defined through its handle can access the content of
variables that exist in the workspace where the anonymous function was created, i.e. it has access to the parameter a. The function file accompanying the script file reads:

## function fvalue $=$ ownrhs $(t, y, a)$

$\%$ the parameter a needs to be in the input list and now the full input list must be $\%$ repeated in the definition of the anonymous function

$$
\text { fvalue }=-a^{*} y+\sin (t) ;
$$

## 20 Example program, time integration

| \% This program computes the numerical solution of dy/dt=f(t,y) with Heun's method (the modified Euler method). |  |  |
| :---: | :---: | :---: |
| \% Filename | : exprog.m |  |
| \% Function-file | : exf.m |  |
| \% Script-files | : exheun.m, extabel.m | ex stands for example |
| \% Screen management: |  |  |
| clear; | \% Clear work memory |  |
| clc; | \% Clear text window |  |
| clf; | \% Clear graphical screen |  |
| $y 0=[1 ; 0]$; | \% Initial condition |  |
| $t 0=0$; | \% Start time |  |
| tend $=5$; | \% End time |  |
| nrsteps $=$ input('G | e the number of steps:'); |  |
| $h=($ tend-t0)/nrste | \% Time step |  |
| exheun | \% Call for the script file containing Heun's method (the modified Euler method) |  |
| extabel | \% Call for the script file designed to print the results |  |
|  | \% The commands from a script file are substituted directly into this program. |  |
| pause(5); | \% The program pauses a while before it shows the graph |  |
| hold on; |  |  |
| plot(tgraph,ygraph(1,:), '-',tgraph,ygraph(2,:), '--'); |  | \% components of y are distinguished by |
|  |  | \% plotting the 2nd component with a broken line |
| axis([t0 tend -5 5]); |  | \% it is preferable to call axis after plot |
| title('Initial value problem: Name compulsory!'); |  |  |
| xlabel(['Solution using Heun for $h=$ ' $\mathbf{n u m 2 s t r}(h)]$ ); |  |  |
| hold off; |  |  |

```
% Heun's method. Script file with filename exheun.m.
% Assuming (t0, y0) "nrsteps" steps are being executed
% The derivative of the diff. eq. is given in the function file exf.m.
% The results are put in tgraph and ygraph
tgraph=zeros(1,nrsteps+1);
ygraph=zeros(length(y0),nrsteps+1);; % create matrix to save results
tgraph(1)=t0;
ygraph (:,1)=y0; % start saving results
y=y0;}t=t0
for j=1:nrsteps
    kl=h*exf(t,y);
    k2=h* exf(t+h,y+kl),
    ynew =y+(kl+k2)/2;
    tnew =t+h;
    tgraph(j+1)=tnew;
    yoraph(:j+1)
    t=tnew;
    y=ynew;
end;
```

| \% Vectorfunction f. Function file with filename exf.m |  |
| :---: | :---: |
| function | yacc $=\operatorname{exf}(t, y) ;$ |
|  | $\begin{array}{r} y a c c=\left[-2^{*} y(1)-y(2)+t ;\right. \\ \left.-y(1)-2^{*} y(2)-t\right] ; \end{array}$ |

```
% Print result. Script file with file name extabel.m.
% The results which are stored in tgraph and ygraph are
% printed in an 8-digit floating-point format in a table.
% In order to make a hardcopy of the tables you need to remove
% the first and the last two comment symbols (%).
% fprintf is actually a C-command
% In the format string of fprintf (the part between quotation marks),
% text which needs to be printed is given, and for every number
% which has to be printed the format is given.
% %5.1f means: fixed-point format with 1 decimal and 5 positions.
% %15.7e means:floating point (exponential) format with }7\mathrm{ decimals and 15 positions.
% In means: continue printing on the next line
% After the format string the variables which (possibly) need to be printed follow.
% the actual file starts now:
% diary output
fprintf('Heun's method, h=%5.3f \n',h);
fprintf('step t y(l)
for k=0:5:nrsteps % % print every 5th result
    fprintf('%4.0f%5.1f%15.7e %15.7e\n',k,tgraph(k+1),ygraph(1:2,k+1)); % the solution y has 2 components:
end;
% diary off
```

| $\%$ Results of the example program |  |  |  |
| :---: | :---: | :---: | :---: |
| Heun's method, $h=0.100$ | $y(1)$ | $y(2)$ |  |
| step | $t$ | $y(1)$ |  |
| 0 | 0.0 | $1.0000000 e+00$ | $0.0000000 e+00$ |
| 5 | 0.5 | $5.2536330 e-01$ | $-2.9586400 e-01$ |
| 10 | 1.0 | $5.7914644 e-01$ | $-5.2647651 e-01$ |
| 15 | 1.5 | $8.4164231 e-01$ | $-8.2955459 e-01$ |
| 20 | 2.0 | $1.2051207 e+00$ | $-1.2023466 e+00$ |
| 25 | 2.5 | $1.6240001 e+00$ | $-1.6233635 e+00$ |
| 30 | 3.0 | $2.0751573 e+00$ | $-2.0750112 e+00$ |
| 35 | 3.5 | $2.5455986 e+00$ | $-2.5455650 e+00$ |
| 40 | 4.0 | $3.0276755 e+00$ | $-3.0276678 e+00$ |
| 45 | 4.5 | $3.5167996 e+00$ | $-3.5167979 e+00$ |
| 50 | 5.0 | $4.0101983 e+00$ | $-4.0101979 e+00$ |

## 21 Example program, filling a penta-diagonal matrix



## 22 Reference and index

In this section the following notation holds:

```
n,m - scalar
A - matrix
v,w,b - vector
x,y - arbitrary
f - user supplied function file
```

| Command | Explanation | Page |
| :---: | :---: | :---: |
| [] | are used for creating matrices and vectors |  |
| () | are used to : <br> - indicate the order of operations <br> - embrace arguments of functions <br> - embrace indices of matrices and vectors |  |
| $\cdots$ | Three or more dots at the end of a line indicate that the line continues on the next line | 9 |
|  | symbol that separates between row elements in a matrix. | 14 |
| ; | symbol that separates between distinct rows in a matrix. We can also use the semicolon to suppress the display of computations on the screen and to separate different commands on a line | 9,14 |
| \% | All text on a line after the symbol $\%$ will be regarded as comment | 9 |
| ! | used to insert operating system commands | 9 |
| : | used for the generation of variables in for-loops and used to select matrix elements: $A(:, n)$ is the $\mathrm{n}^{\text {th }}$ column of $\mathrm{A}, \mathrm{A}(\mathrm{m},:)$ the $\mathrm{m}^{\text {th }}$ row |  |
| , | transposes matrices and vectors | 17 |
| .* | v .* w : multiplication of two vectors by multiplying element by element (operation in array sense) | 7,17 |
| 1 | $\mathrm{A} \backslash \mathrm{b}$ gives the solution of $\mathrm{Ax}=\mathrm{b}$ | 32 |
| $\wedge$ | $x^{\wedge} \mathrm{y}=\mathrm{x}$ to the power y | 12 |
| \& | logical and | 20 |
| 1 | logical or | 20 |
| $\sim$ | logical not | 20 |
| abs | $\mathbf{a b s}(\mathrm{x})$ is the absolute value of (the elements of) x | 13,18 |
| atan | $\operatorname{atan}(\mathrm{x})$ is the arctangent of (the elements of) x | 18 |
| axis | $\operatorname{axis}(\mathrm{v})$, with $\mathrm{v}=[\mathrm{xmin}$ xmax ymin ymax] replaces the automatical scaling of a graph's axes by the configuration given by the vector v . axis ('square') switches over from a rectangular graphical screen to a square-shaped graphical screen, axis ('normal') switches back to the rectangular screen. | 26 |
| chol | chol(A) yields the Cholesky decomposition of the matrix A. | 18,32 |
| clc | clc clears the command window and moves the cursor to the upper left corner | 10 |


| clear | clear clears the variables from the Matlab memory. clear $x\{y\}$ removes the variable x \{and y \} | 10 |
| :---: | :---: | :---: |
| clf | clf clears the graphical window | 10,26 |
| close | close closes the graphical window | 10,26 |
| cos | $\boldsymbol{\operatorname { c o s }}(\mathrm{x})$ is the cosine of (the elements of) x | 18 |
| cputime | cputime determines the cpu time | 10 |
| demo | demo starts a demonstration | 7,10 |
| det | $\boldsymbol{\operatorname { d e t }}(\mathrm{A})$ determinant of A | 18 |
| diag | diag ( $\mathrm{v}, \mathrm{k}$ ) returns a square matrix with the elements of the vector v on the $\mathrm{k}^{\text {th }}$ upper diagonal | 15 |
| diary | diary filename puts all following commands and results in a file with the name filename. This stops after diary off is entered | 23 |
| diff | diff( $\mathrm{f}, \mathrm{x}$ ) differentiates f w.r.t. x | 34 |
| disp | disp('text') writes text on the screen. disp(x) displays the value of the variable x , without variable name | $\begin{gathered} 11,23, \\ 33 \end{gathered}$ |
| double | double(expr) converts the symbolic expression to a number | 34 |
| dsolve | dsolve(deq) solves the differential equation deq | 34,35 |
| eig | $\boldsymbol{e i g}(\mathrm{A})$ computes the eigenvalues and eigenvectors of A | 18 |
| else, elseif | see if | 19 |
| end | end is the command that ends loop statements, conditional statements and nested functions | $\begin{gathered} 19,21, \\ 37 \end{gathered}$ |
| $\exp$ | $\boldsymbol{\operatorname { e x p }}(\mathrm{x})$ is the exponent of (the elements of) x with base e | 18 |
| eye | eye $(\mathrm{n})$ is the nxn identity matrix. eye $(m, n)$ is an mxn matrix with ones on the diagonal and zeros elsewhere | 14 |
| factor | factor(expr) factors the symbolic expression expr | 34 |
| for | ```loop statement: for variable = start value : increment : end value, commands end``` | 7 |
| format | formats the output: <br> format short - 5 digits, fixed point <br> format short e - 5 digits, floating point <br> format long - 15 digits, fixed point <br> format long e - 15 digits, floating point <br> standard configuration is short. <br> format compact suppresses extra empty lines in the output format loose adds empty lines | 11 |
| fplot | $\mathbf{f p l o t}(@ \mathrm{f},[\mathrm{a}, \mathrm{b}])$ plots the function f on [a,b] | 26,36 |
| fprintf | C-command for advanced formatting of output | 23 |
| function | user defined function: <br> function outputvar = functionname (inputvars) commands <br> Function files have to have the name functionname.m. | 29 |
| ginput(n) | gets the coordinates of n points in the graph, which are located by positioning the cursor and thereupon clicking the mouse | 26 |
| global | global x changes x into a global variable | 31 |


| grid | adds a grid (a lattice of horizontal and vertical lines) to a graph | 26 |
| :---: | :---: | :---: |
| help | help shows the functions you can get information about. help functionname shows this information on the screen. helpwin generates an extra window with helptopics | 6,10 |
| hold | hold on keeps the last plot in the graphical screen. A new graph will be plotted on top of the existing one. hold off restores the default settings. In that case, when a plot command has been given, the graphical screen will be cleared before the new graph is be plotted | 26 |
| i | the imaginary unit | 18 |
| if | conditional statement: <br> if statement <br> commands if statement <br> commands  <br> elseelseif statement <br> commands commands  <br> end elsecommands  <br>    <br> end   | 19 |
| imag | imag(c) returns the imaginary part of the complex number c | 13 |
| inf | infinity | 18 |
| input | input('text') displays text on the screen and waits for input by the user. Can be assigned to a variable | 25 |
| int | int (f, $\mathrm{x}, \mathrm{a}, \mathrm{b}$ ) integrates f w.r.t. x from a to b | 34 |
| length | length(v) returns the number of elements of the vector v | 18 |
| linspace | linspace ( $\mathrm{x} 1, \mathrm{x} 2, \mathrm{n}$ ) generates a n -point grid on [ $\mathrm{x} 1, \mathrm{x} 2$ ]; i.e. grid with spacing (x2-x1)/(n-1) | 26 |
| load | load filename loads the variables of the file filename into the memory. The file is of type .mat or of type .txt. | 25 |
| $\log$ | $\log (\mathrm{x})$ is the natural logarithm of (the elements of) x | 18 |
| $\log 10$ | $\log 10(\mathrm{x})$ is the logarithm with base 10 of (the elements of) x | 18 |
| lu | $\mathbf{l u}(\mathrm{A})$ computes the lu factorization of the matrix A | 18,32 |
| max | $\boldsymbol{m a x}(\mathrm{v})$ returns the largest element of the vector v | 18 |
| mesh | mesh( $\mathrm{x}, \mathrm{y}, \mathrm{Z}$ ) plots the matrix Z versus the vectors y and x , creating a mesh | 27 |
| meshgrid | $\operatorname{meshgrid}(\mathrm{x}, \mathrm{y})$ creates a 2D grid from the vectors $\mathrm{x}, \mathrm{y}$ | 27 |
| min | $\boldsymbol{\operatorname { m i n }}(\mathrm{v})$ returns the smallest element of the vector v | 18 |
| norm | norm(v) computes the Euclidean norm of v and norm(v, inf) computes the infinity norm | 18 |
| num2str | num2str(var) converts the number var to a text string | 26 |
| ones | ones( n ) is an nxn matrix filled with ones, ones( $\mathrm{m}, \mathrm{n}$ ) is an mxn matrix | 14 |
| pause | pause pauses the running programme and waits until the user presses any key. pause( n ) pauses during n seconds | 6,10 |
| pi | $\mathbf{p} \mathbf{i}$ is the machine's representation of $\pi$ | 18 |

$\left.\begin{array}{|l|l|c|}\hline \text { plot } & \begin{array}{l}\text { Drawing a graph: } \\ \text { plot(v) } \\ \text { plot(v,w) } \\ \text { plot(m,n,'symbol') } \quad \begin{array}{c}\text { - plot the vector v versus its indices } \\ \text { - put a symbol at position (m,n) in the } \\ \text { graph. The following symbols can be } \\ \text { used: }+ \text {, *, o and x }\end{array}\end{array} & 6,26 \\ \hline \text { plot3 } & \text { plot3(x,y,z) plots a line through the coordinates of vectors x, y, z }\end{array}\right\}$

| while | conditional loop statement: <br> while statement <br> commands <br> end | 21 |
| :--- | :--- | :---: |
| whos | whos shows the name, size and type of the variables in the Matlab <br> memory | 10,12, <br> 33 |
| xlabel | xlabel('text') places text underneath the x-axis of the graphical <br> screen | 26 |
| ylabel | ylabel('text') places text next to the y-axis of the graphical screen | 26 |
| zeros | zeros(n) returns an nxn matrix with zeros; zeros(m,n) returns an <br> mxn matrix | 14 |
| zoom | zoom makes it possible to zoom in at a specific point in the graph <br> by clicking the mouse at that point | 26 |

